

## Note on Sample Design and Estimation Procedure

**1.0 Objective of the survey:** There are primarily two objectives of PLFS. The first is to measure the dynamics in labour force participation and employment status in the short time interval of three months for the urban areas only in the Current Weekly Status (CWS). Thus, in every quarter, PLFS will bring out the level and change estimates of the key labour force indicators in CWS viz. Worker Population Ratio (WPR), Labour Force Participation Rate (LFPR), Unemployment Rate (UR). Secondly, for both rural and urban areas, level estimates of all important parameters in both usual status and CWS will be brought out annually.

### 1.1 Outline of the Survey Programme

**1.1.1 Geographical coverage of the survey:** The survey covers the whole of the Indian Union *except* the villages in Andaman and Nicobar Islands which remain extremely difficult to access throughout the year.

**1.2 Schedules of enquiry:** Following schedules are canvassed:

Schedule 0.0PL	: List of households
Schedule 10.4	: Employment and Unemployment (First Visit)
Schedule 10.4	: Employment and Unemployment (Revisit)

### 1.3 Sample Design

#### 1.3.1 Rotational scheme for pilot survey:

A rotational panel sampling design has been used in urban areas. The rotational scheme is of two years duration to accommodate the changes in the urban frame in the intracensal period; in the sense that the sampling frames for both rural and urban areas will remain unchanged for every two-year duration. In this rotational panel scheme each selected household in urban areas will be visited four times – one with first visit schedule and other three with revisit schedule. The estimates can be given for *successive* quarters without any break in the series (starting from the fifth quarter), *ensuring a 75% matching between consecutive quarters*. The proposed design aims at generating quarterly estimates of level and change parameters of some important labour force indicators (LFPR, WPR & UR) based on CWS data in urban areas and annual estimates of level parameters based on usual status for both rural and urban areas in the line of employment & unemployment survey of NSS quinquennial round.

#### 1.3.2 Rotational panel design for urban areas

- i. The initial rotational panel is for two years, where only 25% FSUs of urban annual allocation will be covered in the first quarter (Panel  $P_{11}$ ) with detail listing and canvassing of visit 1 schedule in the selected households; where  $P_{ij}$  indicates the panel belonging to  $j^{\text{th}}$  quarter of the  $i^{\text{th}}$  two-year period of rotation.

- ii. Another 25% FSUs will be covered in the second quarter (Panel P<sub>12</sub>) for taking up visit 1 schedule and revisit schedule will be canvassed in the selected households of Panel P<sub>11</sub>.
- iii. A new panel P<sub>13</sub> of 25% FSUs will be surveyed in third quarter with visit 1 schedule and revisit schedules will be canvassed in the households of panels P<sub>11</sub> & P<sub>12</sub>.
- iv. In the fourth quarter, households of panels P<sub>11</sub>, P<sub>12</sub> & P<sub>13</sub> will be surveyed with revisit schedule and a new panel P<sub>14</sub> with 25% FSUs for visit 1 schedule.
- v. In the subsequent quarters of second year 75% FSUs (3 panels - P<sub>12</sub>, P<sub>13</sub> & P<sub>14</sub>) will be common and an earlier panel (P<sub>11</sub>) will be replaced by a new panel (P<sub>15</sub>) for canvassing visit 1 schedule. This will continue till 8<sup>th</sup> quarter.
- vi. All the FSUs of the panels P<sub>11</sub>, P<sub>12</sub>, ..., P<sub>18</sub> (each of which is with 25% of FSUs) will be selected before commencement of survey in the first quarter.
- vii. At the end of the second year of each two-year duration, updated frame will be used for both rural and urban areas.
- viii. FSUs of another set of panels P<sub>21</sub>, P<sub>22</sub>, ..., P<sub>28</sub> selected from the updated frame will be made ready before commencement of first quarter of third year (first quarter of the second two-year duration). These panels P<sub>21</sub> to P<sub>28</sub> will take care of the changes in the urban frame during the intracensal period.
- ix. In the ninth quarter (first quarter of the second two-year duration), panel P<sub>21</sub> selected from the updated frame will be introduced and the panels P<sub>16</sub>, P<sub>17</sub> and P<sub>18</sub> of the old frame will be surveyed.
- x. This scheme will continue for another 2 years with the introduction of panels P<sub>22</sub> to P<sub>28</sub> each in one quarter for the subsequent 7 quarters till the end of the fourth year (second year of the two-year period).
- xi. This scheme of rotation of panels will enable generation of estimates of change parameters with 75% matching and 25% of unmatched samples from fifth quarter onwards.
- xii. One of the main advantages of this plan of rotation is that there will not be any break in the series of estimates of the change parameters starting from 5<sup>th</sup> quarter.
- xiii. Since major changes in the rural-urban frame occurs in the Census years (say for the year 2023-24), provision is to be made to generate estimates without break in the series of estimates considering panels from pre and post-census frames.

### 1.3.3 Rural samples

For rural areas, samples for all the 8 quarters have been selected before commencement of survey for each two-year period, while the frame remains same for this duration. In each quarter, only 25% FSUs of annual allocation (as is done in each sub-round of NSS rounds) are being covered in rural areas so that independent estimates can be generated for each quarter. For this purpose, quarterly allocation is multiple of 2 for drawing interpenetrating sub-samples.

***There will not be any revisit in the rural samples.***

1.3.4 The following table gives the rotational panel schemes in tabular format:

	panels for the first 2 year period								panels from updated frame for the next 2 year period			
	During the four quarters of the first year				During the four quarters of the second year				During the four quarters of the third year			
	Qtr1	Qtr2	Qtr3	Qtr4	Qtr1	Qtr2	Qtr3	Qtr4	Qtr1	Qtr2	Qtr3	Qtr4
Urban Panel	P <sub>11</sub> *	P <sub>11</sub>	P <sub>11</sub>	P <sub>11</sub>	P <sub>15</sub> *	P <sub>15</sub>	P <sub>15</sub>	P <sub>15</sub>	P <sub>21</sub> *	P <sub>21</sub>	P <sub>21</sub>	P <sub>21</sub>
		P <sub>12</sub> *	P <sub>12</sub>	P <sub>12</sub>	P <sub>12</sub>	P <sub>16</sub> *	P <sub>16</sub>	P <sub>16</sub>	P <sub>16</sub>	P <sub>22</sub> *	P <sub>22</sub>	P <sub>22</sub>
			P <sub>13</sub> *	P <sub>13</sub>	P <sub>13</sub>	P <sub>13</sub>	P <sub>17</sub> *	P <sub>17</sub>	P <sub>17</sub>	P <sub>17</sub>	P <sub>23</sub> *	P <sub>23</sub>
				P <sub>14</sub> *	P <sub>14</sub>	P <sub>14</sub>	P <sub>14</sub>	P <sub>18</sub> *	P <sub>18</sub>	P <sub>18</sub>	P <sub>18</sub>	P <sub>24</sub> *
Rural	R <sub>11</sub> *	R <sub>12</sub> *	R <sub>13</sub> *	R <sub>14</sub> *	R <sub>15</sub> *	R <sub>16</sub> *	R <sub>17</sub> *	R <sub>18</sub> *	Fresh rural samples in third year from the updated frame			
*Visit 1 schedule will be canvassed												
R <sub>ij</sub> * indicates samples to be covered in rural areas in j <sup>th</sup> quarter of i <sup>th</sup> two-year period												

1.3.5 It is seen from the above table that one panel of urban sample FSUs will be in the sample for 4 quarters and the selected households in an FSU will be surveyed for the successive periods during which the FSU remains in the sample. Selected households will be visited 4 times for canvassing the detailed schedule of enquiry of the PLFS (Schedule 10.4: Employment and Unemployment). These visits are termed as **first visit** and **revisit**. For this, two formats of the detailed schedule of enquiry have been devised viz., Schedule 10.4: Employment and Unemployment (First Visit) and Schedule 10.4: Employment and Unemployment (Revisit).

To implement the rotational scheme in urban areas, when a panel appears for the first time in any quarter with 25% of annual allocation, listing and selection of households will be done in all the selected FSUs in that panel. The first visit schedule will be canvassed in the selected households. The selected FSUs/households will be revisited in the subsequent three quarters as the panel will remain in the sample for four quarters. **During the revisit, listing and selection of households will not be done afresh.** Only the households selected during first visit will be revisited for canvassing revisit schedule. At the time of revisit if any sample household is not found, same may be treated as casualty and a substitute household need not be surveyed. If any sample household is found to have split, then, among the split households available in the FSU/Sub-block, the household where the head/senior most member of the erstwhile household is available will be covered. In the PLFS scheme, each selected household of urban FSUs only will be visited four times, one in each quarter.

1.3.6 **Outline of the design:** A stratified multi-stage design has been adopted. The first stage units (FSU) are the Urban Frame Survey (UFS) blocks in urban areas and 2011 Population Census villages (Panchayat wards for Kerala) in rural areas. The ultimate stage units (USU) are households. As in usual NSS rounds, in the case of large FSUs one intermediate stage unit, called hamlet group/sub-block, will be formed.

**1.3.7 Sampling Frame for First Stage Units:** The list of latest available Urban Frame Survey (UFS) blocks is considered as the urban sampling frame. List of 2011 Population Census villages (Panchayat wards for Kerala) constitutes the rural sampling frame. Since the duration of rotational panel is of two-year, the urban sampling frame once updated incorporating the changes made in the current phase of UFS will remain unchanged for two years. Similarly the rural sampling frame with changes, if any, for urbanisation of village(s) will remain unchanged for two years. After completion of every two-year period, the frames will be updated for incorporating the changes likely to occur during this period. When next Population Census details will be available, the new frame will be used only when UFS blocks for all newly declared Census Towns and Statutory Towns are available for preparation of sampling frame, as the new list of census villages will not include those villages which will be considered as urban areas.

**1.3.8 Stratification:** In urban areas strata have been formed within each NSS region on the basis of size class of towns as per Population Census 2011. The stratum numbers and their composition (within each region) are as follows:

stratum 1 :	all towns with population less than 50,000
stratum 2 :	all towns with population 50,000 or more but less than 3 lakhs
stratum 3 :	all towns with population 3 lakhs or more but less than 15 lakhs
stratum 4, 5, 6,... :	each city with population 15 lakhs or more

The rural areas of each NSS region constitute rural stratum. In case of rural sectors of Nagaland, a special stratum will be formed within the State consisting of all the villages which are difficult to access.

**1.3.9.1 Sub-Stratification: Urban:** In urban areas there is no sub-stratification.

**1.3.9.2 Rural:** 'r/8' sub-strata have been formed in each rural stratum, if 'r' is the annual sample size allocated for a rural stratum. The villages within a stratum as per frame are first arranged in ascending order of population. Then sub-strata 1 to 'r/8' are demarcated in such a way that each sub-stratum comprised a group of villages of the arranged frame and have more or less equal population.

**1.3.10 Total sample size (FSUs):** 12800 FSUs (7024 villages and 5776 UFS blocks) are being covered annually at all-India level.

**1.3.10.1 State/UT level sample size** will be allocated between two sectors in proportion to population as per Census 2011 with double weightage to urban sector in general. Within each sector of a State/UT, the respective sample size has been allocated to the different strata (in the case of urban areas) and strata/ sub-strata (in the case of rural areas) in proportion to the population as per Census 2011. Urban allocations at stratum level have been adjusted to multiples of 8 with a minimum sample size of 8 (for 4 panels, each of size multiple of 2). Rural allocation for each stratum is also multiple of 8 with minimum sample size of 8 (for 4 quarters, each of size

2). For special stratum formed in rural areas of Nagaland as discussed in para 1.3.8, 16 FSUs will be allocated.

1.3.10.2 It may be noted that quarterly allocation of FSUs is same for an NSS state-region although 25% of the urban FSUs rotate over the quarters according to the rotational scheme. However, quarterly allocation of urban FSUs for FOD regions and FOD sub-regions may vary over the quarters since new FSUs entering the sample according to the rotational scheme may or may not belong to the same FOD region or FOD sub-region.

1.3.11 **Selection of first stage units:** Urban FSUs are selected by probability proportional to size with replacement (PPSWR) scheme, size being the number of households in the UFS block. Samples for a panel within each stratum are drawn in the form of two independent sub-samples. To implement the rotational scheme, 4 groups of sample FSUs of equal size (each multiple of size 2, half for each of sub-sample 1 and sub-sample 2) are drawn randomly. In the rural areas, samples for a stratum/sub-stratum are drawn randomly in the form of two independent sub-samples with probability proportional to size with replacement (PPSWR) scheme, size being the population of the village and equal number of samples are allocated among the four quarters.

1.3.12 **Criterion for hamlet-group/ sub-block formation:** After identification of the boundaries of the FSU, it is to be determined whether listing is to be done in the whole sample FSU or not. In case the population of the selected FSU is found to be 1200 or more, it is to be divided into a suitable number (say, D) of ‘hamlet-groups’ in the rural sector and ‘sub-blocks’ in the urban sector by more or less equalising the population as stated below.

approximate present population of the sample FSU	no. of hg's/sb's to be formed
less than 1200 (no hamlet-groups/sub-blocks)	1
1200 to 1799	3
1800 to 2399	4
2400 to 2999	5
3000 to 3599	6
.....and so on	

For rural areas of Himachal Pradesh, Sikkim, Andaman & Nicobar Islands, Uttarakhand (except four districts Dehradun, Nainital, Hardwar and Udham Singh Nagar), Punch, Rajouri, Udhampur, Reasi, Doda, Kishtwar, Ramban, Leh (Ladakh), Kargil districts of Jammu and Kashmir and Idukki district of Kerala, the number of hamlet-groups to be formed as follows:

approximate present population of the sample village	no. of hg's to be formed
less than 600 (no hamlet-groups)	1
600 to 899	3
900 to 1199	4
1200 to 1499	5
1500 to 1799	6
.....and so on	

**1.3.13 Formation and selection of hamlet-groups/ sub-blocks:** In case hamlet-groups/ sub-blocks are to be formed in the sample FSU, the same will be done by more or less equalizing population. Two hamlet-groups (hg)/ sub-blocks (sb) are to be selected from a large FSU wherever hamlet-groups/ sub-blocks will be formed in the following manner – one hg/ sb with maximum percentage share of population will always be selected and termed as hg/ sb ‘1’; one more hg/ sb will be selected from the remaining hg’s/ sb’s by simple random sampling (SRS) and will be termed as hg/ sb ‘2’. Listing and selection of the households will be done independently in the two selected hamlet-groups/ sub-blocks. The FSUs without hg/ sb formation will be treated as sample hg/ sb number ‘1’. It is to be noted that if more than one hg/ sb are found to have same maximum percentage share of population, the one among them which listed first will be treated as hg/ sb ‘1’.

Listing and selection of the households is to be done independently in the two selected hg’s/sb’s.

**1.3.14 Formation of second stage strata and allocation of households:**

1.3.14.1 Second stage stratification (SSS) in each FSU/hg/sb is to be done based on the number of members in each household who have completed secondary level of education considering general type of education. In urban FSUs 4 SSS while in rural FSUs 3 SSS are to be formed in rural areas. Details are given in the following table.

composition of SSS (rural)	SSS	number of members	number of households to be surveyed	
			FSU without hg formation	FSU with hg formation (for each hg)
number of members in the household having level of general education as secondary (10 <sup>th</sup> standard) or above	SSS 1	2 or more	2	1
	SSS 2	1	4	2
	SSS 3	0	2	1
<b>TOTAL</b>			<b>8</b>	
composition of SSS (urban)	SSS	number of members	number of households to be surveyed	
			FSU without sb formation	FSU with sb formation (for each sb)
number of members in the household having level of general education as secondary (10 <sup>th</sup> standard) or above	SSS 1	3 or more	2	1
	SSS 2	2	2	1
	SSS 3	1	2	1
	SSS 4	0	2	1
<b>TOTAL</b>			<b>8</b>	

**1.3.15 Selection of households:** From each SSS the sample households are to be selected by SRSWOR.

## 2. Estimation Procedure

### 2.1 Subscripts

s = subscript for s-th stratum

t = subscript for t-th sub-stratum (**for rural only**)

r = panel number (**for urban only**)

m = subscript for sub-sample (m = 1, 2)

i = subscript for i-th FSU [village (panchayat ward)/ block]

d = subscript for a hamlet-group/ sub-block (d = 1, 2)

j = subscript for j-th second stage stratum in an FSU/ hg/sb [ j = 1, 2, 3 (for rural) or 1, 2, 3, 4 (for urban)]

k = subscript for k-th sample household under a particular second stage stratum within an FSU/ hg/sb

D = total number of hg's/ sb's formed in the sample FSU

$D^* = 0$  if  $D = 1$

= (D – 1) for FSUs with  $D > 1$

Z = total size of a rural/urban stratum/sub-stratum (= sum of sizes for all the FSUs of a stratum/sub-stratum)

z = size of sample village/UFS block used for selection

n = number of sample FSUs surveyed including 'uninhabited' and 'zero cases' but excluding casualty for a particular sub-sample and stratum/sub-stratum/panel

H = total number of households listed in a second-stage stratum of an FSU / hamlet-group or sub-block of sample FSU

h = number of households surveyed in a second-stage stratum of an FSU / hamlet-group or sub-block of sample FSU

x, y = observed value of characteristics x, y under estimation

$\hat{X}$ ,  $\hat{Y}$  = estimate of population total X, Y for the characteristics x, y

Under the above symbols,

$y_{srmidjk}$  = observed value of the characteristic y for the  $k^{\text{th}}$  household in the  $j^{\text{th}}$  second stage stratum of the  $d^{\text{th}}$  hg/ sb (d = 1, 2) of the  $i^{\text{th}}$  **urban** FSU belonging to the  $m^{\text{th}}$  sub-sample of the  $r^{\text{th}}$  panel of  $s^{\text{th}}$  stratum

$y_{stmidjk}$  = observed value of the characteristic y for the  $k^{\text{th}}$  household in the  $j^{\text{th}}$  second stage stratum of the  $d^{\text{th}}$  hg/ sb (d = 1, 2) of the  $i^{\text{th}}$  **rural** FSU belonging to the  $m^{\text{th}}$  sub-sample of the  $t^{\text{th}}$  sub-stratum of  $s^{\text{th}}$  stratum

However, for ease of understanding, a few subscripts have been suppressed in following paragraphs where they are obvious.



**3. Formulae for Quarterly Estimates of Aggregates for a particular stratum × panel × sub-sample of the urban sector from Schedule 10.4:**

3.1 The estimate for a **stratum × panel × sub-sample** may be obtained as follows:

$$\hat{Y}_{srm} = \frac{Z_s}{n_{srm}} \sum_{i=1}^{n_{srm}} \frac{1}{z_{srmi}} \left[ \sum_{j=1}^4 \frac{H_{srmi1j}}{h_{srmi1j}} \sum_{k=1}^{h_{srmi1j}} y_{srmi1jk} + D_{srmi}^* \sum_{j=1}^4 \frac{H_{srmi2j}}{h_{srmi2j}} \sum_{k=1}^{h_{srmi2j}} y_{srmi2jk} \right]$$

3.2 The estimate for aggregates for a particular **stratum × panel** based on two sub-samples may be obtained as:

$$\hat{Y}_{sr} = \frac{1}{2} \sum_{m=1}^2 \hat{Y}_{srm}$$

3.3 The estimate for aggregates for a particular stratum based on ‘**r**’ **panels** and two sub-samples may be obtained as:

$$\hat{Y}_s = \frac{1}{r} \sum_r \hat{Y}_{sr}, r = 1, 2, 3, 4$$

( r will be ‘4’ from fourth quarter and r may be less than ‘4’ till third quarter)

3.4 From fourth quarter onwards, estimate for aggregates for a particular stratum based on all the 4 panels and two sub-samples may be generated as:

$$\hat{Y}_s = \frac{1}{4} \sum_{r=1}^4 \hat{Y}_{sr}$$

3.5 Estimate of an aggregate character for a State may be obtained by summing the stratum estimates as follows:

$$\hat{Y} = \sum_s \hat{Y}_s$$

3.6 Let  $\hat{Y}$  and  $\hat{X}$  be the estimates of the aggregates Y and X for two characteristics y and x respectively at the State/ UT/ all-India level. Estimate of a ratio  $R = \frac{Y}{X}$  at State level may be

obtained as the ratio of aggregates of two characters at State levels:  $\hat{R} = \frac{\hat{Y}}{\hat{X}}$

3.7 The estimates of change over the quarters will be measured by the simple difference between the estimates of aggregates or ratios of the corresponding quarters.

**3.8 Estimates of Error:** The estimated variances of the above estimates will be as follows:

**3.8.1 For aggregate  $\hat{Y}$ :**

$$Var(\hat{Y}) = \sum_s \sum_{r=1}^4 Var\left(\frac{1}{4}\hat{Y}_{sr}\right) = \frac{1}{16} \sum_{r=1}^4 \sum_s Var(\hat{Y}_{sr}) \quad \text{where}$$

$Var(\hat{Y}_{sr}) = \frac{1}{4}(\hat{Y}_{sr1} - \hat{Y}_{sr2})^2$ , where  $\hat{Y}_{sr1}$  and  $\hat{Y}_{sr2}$  are the estimates for sub-sample 1 and sub-sample 2 respectively for stratum 's' and panel 'r'.

**3.8.2 For ratio  $\hat{R}$ :**

$$MSE(\hat{R}) = \frac{1}{4\hat{X}^2} \sum_s \left[ (\hat{Y}_{s1} - \hat{Y}_{s2})^2 + \hat{R}^2 (\hat{X}_{s1} - \hat{X}_{s2})^2 - 2\hat{R}(\hat{Y}_{s1} - \hat{Y}_{s2})(\hat{X}_{s1} - \hat{X}_{s2}) \right]$$

where  $\hat{Y}_{s1} = \frac{1}{4} \sum_{r=1}^4 \hat{Y}_{sr1}$  and  $\hat{Y}_{s2} = \frac{1}{4} \sum_{r=1}^4 \hat{Y}_{sr2}$ ;

$\hat{X}_{s1} = \frac{1}{4} \sum_{r=1}^4 \hat{X}_{sr1}$  and  $\hat{X}_{s2} = \frac{1}{4} \sum_{r=1}^4 \hat{X}_{sr2}$

**3.9 Estimates of Relative Standard Error (RSE):**

$$RSE(\hat{Y}) = \frac{\sqrt{Var(\hat{Y})}}{\hat{Y}} \times 100$$

$$RSE(\hat{R}) = \frac{\sqrt{MSE(\hat{R})}}{\hat{R}} \times 100$$

**3.10 For urban samples,** multipliers for panel 'r' will be as follows:

sch.	sector	formula for multipliers	
		segment 1	segment 2
10.4	urban	$\frac{Z_s}{n_{srm}} \times \frac{1}{z_{srmi}} \times \frac{H_{srmi1j}}{h_{srmi1j}}$	$\frac{Z_s}{n_{srm}} \times \frac{1}{z_{srmi}} \times D_{srmi}^* \times \frac{H_{srmi2j}}{h_{srmi2j}}$
j = 1, 2, 3, 4			

**4. Formulae for Annual Estimates of Aggregates for a particular sub-sample and stratum × sub-stratum in the rural/urban sector from Schedule 10.4:**

**4.1 For rural:**

4.1.1 For rural areas, annual estimates of aggregates may be obtained from the data collected in four quarters.

(i) For  $j^{\text{th}}$  second-stage stratum of a stratum × sub-stratum, for a particular sub-sample:

$$\hat{Y}_{stmj} = \frac{Z_{st}}{n_j} \sum_{i=1}^{n_j} \frac{1}{z_{stmi}} \left[ \frac{H_{stmi1j}}{h_{stmi1j}} \sum_{k=1}^{h_{stmi1j}} y_{stmi1jk} + D_{stmi}^* \times \frac{H_{stmi2j}}{h_{stmi2j}} \sum_{k=1}^{h_{stmi2j}} y_{stmi2jk} \right]$$

(ii) For all second-stage strata combined:

$$\hat{Y}_{stm} = \sum_j \hat{Y}_{jstm}$$

**4.1.2 Estimate for aggregates for a sub-stratum:**

Estimate for aggregates for a sub-stratum ( $\hat{Y}_{st}$ ) based on two sub-samples in a sub-stratum is obtained as:

$$\hat{Y}_{st} = \frac{1}{2} \sum_{m=1}^2 \hat{Y}_{stm}$$

**4.1.3 Estimate for aggregates for a stratum:**

Estimate for a stratum ( $\hat{Y}_s$ ) will be obtained as

$$\hat{Y}_s = \sum_t \hat{Y}_{st}$$

**4.1.4 Estimate of Aggregates at State/UT/all-India level:**

The estimate  $\hat{Y}$  at the State/ UT/ all-India level is obtained by summing the stratum estimates  $\hat{Y}_s$  over all strata belonging to the State/ UT/ all-India.

**4.1.5 Estimates of Ratios:**

Let  $\hat{Y}$  and  $\hat{X}$  be the estimates of the aggregates Y and X for two characteristics y and x respectively at the State/ UT/ all-India level.

Then the combined ratio estimate ( $\hat{R}$ ) of the ratio ( $R = \frac{Y}{X}$ ) will be obtained as  $\hat{R} = \frac{\hat{Y}}{\hat{X}}$

**4.1.6 Estimates of Error:** The estimated variances of the above estimates will be as follows:

**4.1.6.1 For aggregate  $\hat{Y}$ :**

$$V\hat{a}r(\hat{Y}) = \sum_s V\hat{a}r(\hat{Y}_s) = \sum_s \sum_t V\hat{a}r(\hat{Y}_{st}) \text{ where } V\hat{a}r(\hat{Y}_{st}) \text{ is given by}$$

$V\hat{a}r(\hat{Y}_{st}) = \frac{1}{4}(\hat{Y}_{st1} - \hat{Y}_{st2})^2$ , where  $\hat{Y}_{st1}$  and  $\hat{Y}_{st2}$  are the estimates for sub-sample 1 and sub-sample 2 respectively for stratum 's' and sub-stratum 't'.

**4.1.6.2 For ratio  $\hat{R}$ :**

$$M\hat{S}E(\hat{R}) = \frac{1}{4\hat{X}^2} \sum_s \sum_t \left[ (\hat{Y}_{st1} - \hat{Y}_{st2})^2 + \hat{R}^2 (\hat{X}_{st1} - \hat{X}_{st2})^2 - 2\hat{R}(\hat{Y}_{st1} - \hat{Y}_{st2})(\hat{X}_{st1} - \hat{X}_{st2}) \right]$$

**4.1.6.3 Estimates of Relative Standard Error (RSE):**

$$R\hat{S}E(\hat{Y}) = \frac{\sqrt{V\hat{a}r(\hat{Y})}}{\hat{Y}} \times 100$$

$$R\hat{S}E(\hat{R}) = \frac{\sqrt{M\hat{S}E(\hat{R})}}{\hat{R}} \times 100$$

**4.2 For urban:**

4.2.1 Considering first visit schedules for each of the four panels of four quarters, annual estimates of aggregates for a **particular sub-sample and stratum** may be obtained for urban areas. For rural areas, annual estimates of aggregates may be obtained from the data collected in four quarters.

(i) For  $j^{\text{th}}$  second-stage stratum of a stratum, for a particular sub-sample:

$$\hat{Y}_{smj} = \frac{Z_s}{n_j} \sum_{i=1}^{n_j} \frac{1}{z_{smi}} \left[ \frac{H_{smi1j}}{h_{smi1j}} \sum_{k=1}^{h_{smi1j}} y_{smi1jk} + D_{smi}^* \times \frac{H_{smi2j}}{h_{smi2j}} \sum_{k=1}^{h_{smi2j}} y_{smi2jk} \right]$$

(ii) For all second-stage strata combined:

$$\hat{Y}_{sm} = \sum_j \hat{Y}_{j sm}$$

**4.2.2 Estimate for Aggregates for a stratum:**

Estimate for aggregates for a stratum ( $\hat{Y}_s$ ) based on two sub-samples in a stratum is obtained as:

$$\hat{Y}_s = \frac{1}{2} \sum_{m=1}^2 \hat{Y}_{sm}$$

**4.2.3 Estimate of Aggregates at State/UT/all-India level:**

The estimate  $\hat{Y}$  at the State/ UT/ all-India level is obtained by summing the stratum estimates  $\hat{Y}_s$  over all strata belonging to the State/ UT/ all-India.

**4.2.4 Estimates of Ratios:**

Let  $\hat{Y}$  and  $\hat{X}$  be the estimates of the aggregates Y and X for two characteristics y and x respectively at the State/ UT/ all-India level.

Then the combined ratio estimate ( $\hat{R}$ ) of the ratio ( $R = \frac{Y}{X}$ ) will be obtained as  $\hat{R} = \frac{\hat{Y}}{\hat{X}}$

**4.2.5 Estimates of Error:** The estimated variances of the above estimates will be as follows:

**4.2.5.1 For aggregate  $\hat{Y}$ :**

$$V\hat{a}r(\hat{Y}) = \sum_s V\hat{a}r(\hat{Y}_s) \text{ where } V\hat{a}r(\hat{Y}_s) \text{ is given by}$$

$V\hat{a}r(\hat{Y}_s) = \frac{1}{4}(\hat{Y}_{s1} - \hat{Y}_{s2})^2$ , where  $\hat{Y}_{s1}$  and  $\hat{Y}_{s2}$  are the estimates for sub-sample 1 and sub-sample 2 respectively for stratum 's'.

**4.2.5.2 For ratio  $\hat{R}$ :**

$$M\hat{S}E(\hat{R}) = \frac{1}{4\hat{X}^2} \sum_s [(\hat{Y}_{s1} - \hat{Y}_{s2})^2 + \hat{R}^2(\hat{X}_{s1} - \hat{X}_{s2})^2 - 2\hat{R}(\hat{Y}_{s1} - \hat{Y}_{s2})(\hat{X}_{s1} - \hat{X}_{s2})]$$

**4.2.5.3 Estimates of Relative Standard Error (RSE):**

$$R\hat{S}E(\hat{Y}) = \frac{\sqrt{V\hat{a}r(\hat{Y})}}{\hat{Y}} \times 100$$

$$R\hat{S}E(\hat{R}) = \frac{\sqrt{M\hat{S}E(\hat{R})}}{\hat{R}} \times 100$$

### 5. Multipliers:

The formulae for multipliers at stratum/sub-stratum/second-stage stratum level for a sub-sample are given below:

schedule	sector	formula for multipliers	
		hg / sb 1	hg / sb 2
10.4	rural	$\frac{Z_{st}}{n_{stmj}} \times \frac{1}{z_{smi}} \times \frac{H_{smi1j}}{h_{smi1j}}$	$\frac{Z_{st}}{n_{stmj}} \times \frac{1}{z_{smi}} \times D_{smi}^* \times \frac{H_{smi2j}}{h_{smi2j}}$
	j = 1, 2, 3 for rural		
	urban	$\frac{Z_s}{n_{smj}} \times \frac{1}{z_{smi}} \times \frac{H_{smi1j}}{h_{smi1j}}$	$\frac{Z_s}{n_{smj}} \times \frac{1}{z_{smi}} \times D_{smi}^* \times \frac{H_{smi2j}}{h_{smi2j}}$
	j = 1, 2, 3, 4 for urban		

**Note:**

- (i) For estimating any characteristic for any domain not specifically considered in sample design, indicator variable may be used.
- (ii) Multipliers have to be computed on the basis of information available in the listing schedule irrespective of any misclassification observed between the listing schedule and detailed enquiry schedule.

### 6. Treatment for zero cases, casualty cases etc.:

6.1 While counting the number of FSUs surveyed ( $n_{sm}$  or  $n_{stm}$ ) in a stratum/sub-stratum, all the FSUs with survey codes 1 to 6 in Schedule 0.0PL will be considered. In addition, if no SSU is available in the frame for Schedule 10.4, then also that FSU will be treated as surveyed in respect of that schedule. However, if SSUs are available in the frame of the FSU but none of these could be surveyed then that FSU has to be treated as casualty and it will not be treated as surveyed in respect of Schedule 10.4.

6.2 *Casualty cases:* FSUs with survey code 7 as per Schedule 0.0PL are treated as casualties. In addition to this, an FSU, although surveyed, may have to be treated as casualty for Schedule 10.4 and a particular *second stage stratum* as given in the following para:

6.2.1 FSUs with survey codes 1 or 4 as per Schedule 0.0PL having number of households in the frame of  $j^{th}$  second stage stratum greater than 0 but number of households surveyed according to data file, considering both hg/sb together, as nil (i.e.  $H_{i1j} + H_{i2j} > 0$  but  $h_{i1j} + h_{i2j} = 0$ ) will be taken as casualties for  $j^{th}$  second stage stratum.

*All the FSUs with survey codes 1 to 6 as per Schedule 0.0PL minus the number of casualties as identified above will be taken as the number of surveyed FSUs ( $n_{stmj}$ ) for that (stratum/sub-stratum)  $\times$  (second stage stratum).*

When casualty for  $j^{\text{th}}$  second stage stratum occurs for a particular hg/sb but not for the other hg/sb, the FSU will not be treated as casualty but some adjustments in the value of H for the other hg/sb will be done as follows:

- (i) Suppose for hg/sb 1,  $H_{i1j} > 0$  but  $h_{i1j} = 0$  while for hg/sb 2,  $H_{i2j} > 0$  and  $h_{i2j} > 0$ . In that case  $D_i^* \times H_{i2j}$  will be replaced by  $(H_{i1j} + D_i^* \times H_{i2j})$  in the formula for multiplier of hg/sb 2.
- (ii) Suppose for hg/sb 1,  $H_{i1j} > 0$  and  $h_{i1j} > 0$  while for hg/sb 2,  $H_{i2j} > 0$  but  $h_{i2j} = 0$ . In that case  $H_{i1j}$  will be replaced by  $(H_{i1j} + D_i^* \times H_{i2j})$  in the formula for multiplier of hg/sb 1.

It may be noted that  $n_{smj}$  or  $n_{stmj}$  would be same for segment 1 & 2 of an FSU.

## 7. Treatment in cases of void second-stage strata/sub-strata /strata at FSU or household level:

7.1 A stratum/sub-stratum may be void because of the casualty of all the FSUs belonging to the stratum/sub-stratum. This may occur in one sub-sample or in both the sub-samples. If it relates to only one sub-sample, then estimate for the void stratum/sub-stratum may be replaced with the estimate as obtained from the other sub-sample for the same stratum/sub-stratum.

7.2 When a stratum/sub-stratum is void in both the sub-samples, the following procedure is recommended:

*Case (I): Stratum/Sub-stratum void cases at FSU levels (i.e. all FSUs having survey code 7):*

- (i) If a rural/urban sub-stratum is void then it may be merged with the other sub-stratum of the stratum.
- (ii) If a rural/urban stratum is void due to all FSUs being casualty, it may be excluded from the coverage of the survey. The state level estimates will be based on the estimates of districts for which estimates are available and remarks to that effect may be added in appropriate places.

*Case (II): Stratum/Sub-stratum void case at second stage stratum level (i.e. all the FSUs were casualties for a particular second stage stratum):*

An FSU may be a casualty for a particular *second stage stratum* although survey code was not 7. If all the FSUs of a stratum/sub-stratum become casualties in this manner for a particular *second stage stratum*, the stratum/sub-stratum will become void. In such cases, the void second stage stratum will be merged with the nearby second stage stratum within the FSU.

**8. Reference to the values of  $Z_{st}$ ,  $n_s$ ,  $z_{sti}$ ,  $D_{sti}$ ,  $D^*_{sti}$ ,  $D_{si}$ ,  $D^*_{si}$ ,  $H_{sti1j}$ ,  $h_{sti1j}$ ,  $H_{sti2j}$ ,  $h_{sti2j}$ :**

- (a) Values of  $Z_{st}$  and the number of FSUs allotted for the whole round are given in Appendix Table 2 for rural sector and in Appendix Table 3 for urban sector.
- (b) Surveyed number of FSUs ( $n_{st}$ ) should not be taken from the tables. The value of  $n_{stm}$  for each sub-sample is to be obtained following the guidelines given in para 6 above. It includes uninhibited and zero cases but excludes casualty cases.
- (c) The value of  $z_{sti}$  for the samples selected by PPS is to be taken from the column of sample list under the heading 'frame population' for rural samples and 'block size' i.e. total number of households in each UFS block for urban samples.
- (d) Value of  $D_{sti}$  is to be taken from item 14 of Block 1, Schedule 0.0PL.  $D^*_{sti}$  is to be calculated from the value of  $D_{sti}$ .
- (e) Values of  $H_{sti1j}$ ,  $H_{sti2j}$  are to be taken from column (5), Block 6 of Schedule 0.0PL for respective segment and second-stage stratum.
- (f) The value of  $h_{sti1j}$  and  $h_{sti2j}$  should not be taken from column (9), Block 6 of Schedule 0.0PL. The figures should be obtained by counting the number of households available in the data file excluding the casualty households.



**Table 1: allocation of sample villages and blocks for PLFS**

State/UT	number of sample villages/blocks		
	total	rural	urban
(1)	(2)	(3)	(4)
ANDHRA PRADESH	496	272	224
ARUNACHAL PRADESH	216	136	80
ASSAM	440	328	112
BIHAR	568	400	168
CHHATTISGARH	280	176	104
GOA	56	24	32
GUJARAT	440	208	232
HARYANA	328	168	160
HIMACHAL PRADESH	256	208	48
JAMMU & KASHMIR	424	240	184
JHARKHAND	344	208	136
KARNATAKA	520	224	296
KERALA	568	264	304
MADHYA PRADESH	584	336	248
MAHARASHTRA	1008	448	560
MANIPUR	320	160	160
MEGHALAYA	160	104	56
MIZORAM	192	64	128
NAGALAND	128	72	56
ODISHA	496	360	136
PUNJAB	400	192	208
RAJASTHAN	528	312	216
SIKKIM	96	56	40
TAMIL NADU	832	392	440
TELANGANA	360	160	200
TRIPURA	232	152	80
UTTAR PRADESH	1136	728	408
UTTARAKHAND	216	120	96
WEST BENGAL	800	424	376
A & N ISLANDS	64	32	32
CHANDIGARH	48	8	40
D & N HAVELI	24	8	16
DAMAN & DIU	16	8	8
DELHI	128	8	120
LAKSHADWEEP	24	8	16
PUDUCHERRY	72	16	56
<b>ALL- INDIA</b>	<b>12800</b>	<b>7024</b>	<b>5776</b>